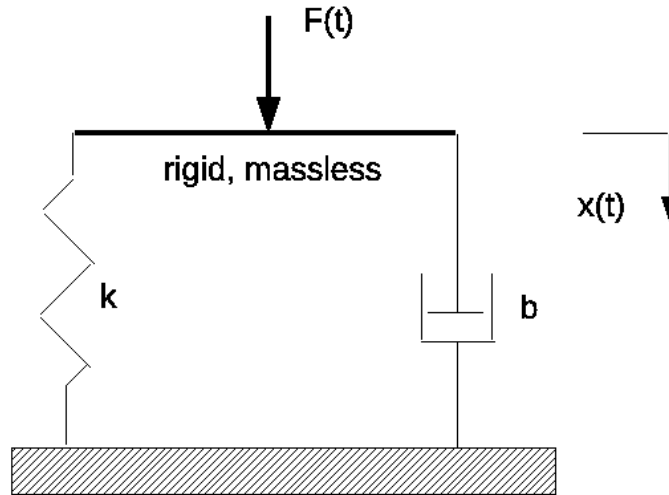


COEN 45, Spring 2010  
Homework #8  
Spring-damper system  
Due Tues. May 25

The figure shows a spring (force proportional to extension) and a damper (force proportional to extensional velocity) connecting a rigid bar to ground.



A force  $F(t)$  is applied vertically. Masses are insignificant, so the equation of motion is

$$b\dot{x} + kx = F(t)$$

subject to an initial condition  $x(0) = x_0$ . You are to solve this differential equation for various conditions using `ode45`. In addition to  $x(t)$  you will plot the damper force  $F_b = b\dot{x}$  and the spring force  $F = kx$ .

1. Write a function for `ode45` to use in its solution process:

```
function xdot = xdot_bk(t,x,etc)
%
% find xdot given t,x
% etc contains [b k load_type period amplitude]
% load_type is 1, 2 or 3
% period is for load_type 2 or 3
% amplitude of load
%
```

Your function should be vectorized, i.e., it should work when  $t$  and  $x$  are either vectors or scalars. A template is available on the class web site.

2. A incomplete driver script `hw8.m` is available on the class web site. It uses your `xdot_bk` to generate and plot responses for various load cases:

- (a)  $x$  versus  $t$
- (b)  $F_b$  versus  $t$
- (c)  $F_k$  versus  $t$

For  $F_b$  you will need  $\dot{x}(t)$ . Assuming you have vectorized your `xdot_bk` you can use it.

- (a) Run the script for load case 1 (`kase = 1`).
- (b) Uncomment the line for case 2 and re-run.
- (c) Uncomment the line for case 3 and re-run.

3. Print each of the plots and on each one, write a comment about the relationship between  $F_k$  and  $F_b$ .

4. Submit three plots plus `hw8.m` and `xdot_bk.m`