

COEN 45  
Winter Quarter, 2011  
Homework #8  
Due Thurs. Mar. 10

Note on `trapz`: The proper way to do integration with `trapz` is *not* what I showed in class, but rather `y=trapz(x,f)` where  $x$  is your vector of independent variables and  $f$  is the corresponding vector of function values. Thus to do

$$\int_0^{2\pi} \cos^2 x \, dx$$

do

```
x = linspace(0,2*pi,100);  
y = trapz(x,cos(x).^2)
```

and the answer is  $y = \pi$

1. Problem 27, p. 318 (3rd. ed: prob. 18, p. 310): orbit of Pluto. Use `trapz` to do the integration, or any MATLAB method of your choice.
2. Problem 33, p. 320 (3rd. ed: prob. 23, p. 311): the well-known von Bertalanffy fish growth model. Use `ode45`:

```
[t,N] = ode45(@bertalanffy,t,N0,[],a,b);
```

3. Newton's law of gravitation says that the attractive force between two masses falls off as the square of the distance between them. The gravitational acceleration experienced by a body at altitude  $h$  above the earth is

$$g = g_0 \frac{R^2}{(R+h)^2}$$

where  $g_0$  is the surface acceleration, 9.81 m/sec<sup>2</sup>, and  $R$  is the radius of the earth, 6371 km.

- (a) An astronaut who ascends into an orbit at altitude of 800 km loses what fraction of his weight?
- (b) If this fraction is not very large, why are astronauts and other objects in orbit said to be weightless?
- (c) The amount of gravitational potential energy gained by the astronaut by ascending into an orbit of altitude  $a$  is

$$U = \int_0^a m g(h) \, dh$$

Calculate this energy in MJ for an astronaut weighing 125 kg (including gear) and an 800-km orbit. (Answer: 871.6)